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A Machine Learning Scheme For Estimating The Diameter of Reinforcing Bars Using Ground Penetrating Radar

Iraklis Giannakis, Antonios Giannopoulos, and Craig Warren

Abstract—Ground Penetrating Radar (GPR) is a well-established tool for detecting and locating reinforcing bars (rebars) in concrete structures. However, using GPR to quantify the diameter of rebars is a challenging problem that current processing approaches fail to tackle. To that extent, we have developed a novel machine learning framework that can estimate the diameter of the investigated rebar within the resolution range of the employed antenna. The suggested approach combines neural networks and a random forest regression, and has been trained entirely using synthetic data. Although the training process relied only on numerical training sets, nonetheless, the suggested scheme is successfully evaluated with real data indicating the generalization capabilities of the resulting regression. The only required input of the proposed technique is a single A-scan, avoiding laborious measurement configurations and multi-sensor approaches. Additionally, the results are provided in real-time making this method practical and commercially appealing.

Index Terms—GPR, rebar, machine learning, random forest, regression, diameter, concrete, non-destructive testing, NDT.

I. INTRODUCTION

GROUND Penetrating Radar (GPR) is a non-destructive technique (NDT) with a unique span of applications [1], ranging from glaciology [2], tree monitoring [3] and archaeology [4], to landmine detection [5], forensic science [6], and planetary exploration [7]. GPR has been established as a mainstream NDT tool in civil engineering [8], and it has been successfully applied for building inspection and for detecting reinforcing bars (rebars) in concrete structures [9]. Various approaches using GPR have been suggested for locating and characterising rebars [10], [11], and there are many commercial GPR systems that are custom-built for this purpose [12], [13]. Although GPR can reliably detect and locate rebars, assessing their quality and estimating their diameter is an ongoing area of research with, as of yet, no conclusive outcomes. Due to that, additional NDT methods (e.g. eddy current [11], electromagnetic induction [14], [15]) need to be applied in the field to complement GPR, raising the overall computational and operational costs, and adding complexity to the acquisition.

To address these issues, various signal processing approaches have been reported that try to establish a causal relationship between the diameter of the rebar and the received GPR signal [10], [16], [17]. However, these methods are based on simplified assumptions and they fail to provide a universal and reliable solution [11]. To tackle this, a detection algorithm based on full-waveform inversion (FWI) using shuffled complex evolution optimization has been suggested [18]. FWI is

a holistic approach that keeps simplifications to a minimum and exploits all the available information embedded in the investigated signal. This gives rise to a robust detection tool that accurately manages to recover both the coordinates and the diameter of buried cylindrical targets [18]. Nonetheless, FWI is a time-consuming process, primarily due to the large computational resources necessary for the numerical evaluation of Maxwell's equations. Machine learning (ML) is gaining a renewed reputation within the GPR community due to the ability to provide real-time results for complex and computationally demanding problems [19], [20], [21]. In that context, a novel forward solver based on ML is described in [11]. A deep neural network (NN) is used in order to map the received waveform with respect to the depth of the rebar, the radius of the rebar, and the water fraction of the concrete [11]. The resulting forward solver is substantially faster than traditional electromagnetic numerical methods [11], and can accelerate FWI without compromising its accuracy [11]. In spite of that, interpretation is still far from real-time, since the ML-based forward solver needs to be coupled with a global optimizer in order to avoid local minima that are present in the optimization space [11].

In this paper a machine learning architecture is suggested in order to map the relationship between a single A-Scan and the diameter of the underlying rebar without the need for FWI. The suggested scheme consists of two NNs and one random forest (RF) regression [22] that are coupled together to estimate the diameter of the rebar in real-time. Similar to [11], the proposed ML framework is trained entirely using synthetic training sets. The generalization capabilities of this method are successfully tested using both numerical and real data.

II. METHODOLOGY

A. Training Set

Supervised ML exploits information from labelled data in order to map the causal relationship (if there is one) between given inputs and their corresponding outputs [23]. To that extent, a well-labelled, coherent and equally distributed training set is crucial during the training process and largely affects the overall performance of ML [23]. For estimating the diameter of rebars, obtaining such a training set from real-data is time-consuming and not practical since it would require casting hundreds of concrete slabs with different water contents and different rebar characteristics. To overcome this,

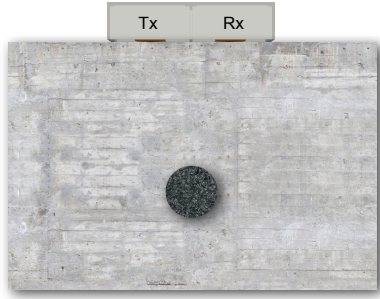


Fig. 1. The simulated scenario used for training the regression scheme. The antenna is the model-equivalent of the GSSI 1.5 GHz antenna [13] and is placed directly above the rebar. The polarization of the antenna is parallel to the main axis of the rebar.

we employ a synthetic training set ensuring accurate labelling and avoiding unattainable experimental setups and undersized training sets.

The training data are generated using the ML-based forward solver described in [11]. The ML-based forward solver uses a deep NN architecture that accurately predicts the simulated A-Scan based on the depth of the rebar, the diameter of the rebar, and the water fraction of the host concrete [11]. The ML solver is trained based on data generated using gprMax [24], [25] – an open source electromagnetic simulator based on a second-order accurate finite-difference time-domain (FDTD) method [26]. The antenna used in the simulations is a model-equivalent of a 1.5 GHz commercial GPR antenna made by Geophysical Survey Systems, (GSSI) [13]. Consequently, the proposed regression scheme is tuned for the GSSI 1.5 GHz antenna, and therefore using a different antenna system would require a new training set to be generated including a new model of that antenna. Figure 1 illustrates the scenario under consideration during the training process. The GSSI 1.5 GHz antenna is placed directly above the rebar on the surface of the concrete. Using a single A-Scan as input instead of a complete B-Scan makes the process practical in the field and reduces the computational requirements necessary to generate the synthetic training data. This configuration (single A-Scan) contains adequate information to fully recover the depth and the radius of the investigated rebar. The direct coupling provides information regarding the dielectric properties of the host medium while the amplitude and the arrival time of the reflected wave are associated with the depth and radius of the rebar. In particular, concrete slabs with higher water fractions act as a low pass filter which results in smoother cross-coupling. In addition, the reflection arrival time is associated with the water fraction of the concrete (derived from cross-coupling) and the depth of the target. Lastly, the amplitude of the reflected signal is related to the water fraction of the concrete (derived from the cross-coupling), the depth of the target (derived from the cross-coupling and the arrival time of the reflected wave) and the radius of the rebar. In conclusion, a combined sequential approach that utilises all the available information embedded in an A-Scan is capable of estimating the diameter of the rebar within the resolution of the employed antenna [11].

TABLE I
EXTENDED DEBYE PROPERTIES OF CONCRETE [28]

WC	ϵ_s	ϵ_∞	t_0 (ns)	σ ($\Omega^{-1}m^{-1}$)
12 %	12.84	7.42	0.611	20.6×10^{-3}
9.3 %	11.19	7.2	0.73	23×10^{-3}
6.2 %	9.14	5.93	0.8	6.7×10^{-3}
5.5 %	8.63	6.023	1	5.15×10^{-3}
2.8 %	6.75	5.503	2.28	2.03×10^{-3}
0.2 %	4.814	4.507	0.82	6.06×10^{-4}

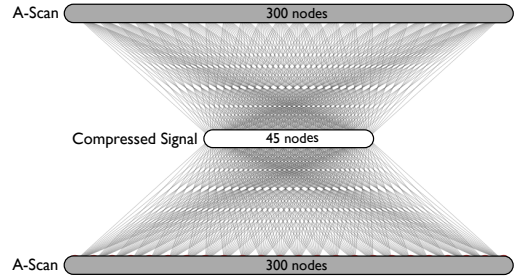


Fig. 2. The structure of the autoencoder used in this work. The inputs and the outputs are the raw A-Scans which consist of 300 points. The inner layer consists of 45 ReLU nodes that represent the compressed A-Scan.

The rebar is modelled as a cylindrical perfect electrical conductor (PEC) with its main axis parallel to the polarization of the antenna. The dielectric properties of concrete are dispersive (similar to natural media [27]) and can be sufficiently approximated using an extended Debye model [11], [28]. The parameters of the Debye model –static permittivity, permittivity at infinite frequency, relaxation time, and conductivity– are expressed only with respect to the water content of the concrete [11], [28]. This is particularly attractive since it reduces the number of parameters necessary to fully describe the dielectric behaviour of the host medium [11]. Table I illustrates the experimentally derived [28] properties of the extended Debye model with respect to the water fraction of the concrete. In a similar approach to [11], a spline interpolation is used in order to map the discrete properties shown in Table I in a continuous manner.

A training set consisting of 2000 samples has proven adequate for accurately resolving the investigated feature space. Increasing the number of samples beyond this value does not seem to affect the overall performance of the regression model. Each trace is simulated using a randomly selected set of the following three parameters:

- Water content of concrete (WC)
- Radius of the rebar (R)
- Depth of the rebar (D)

Based on what is realistically expected in the field [11], the radius and the depth of the rebar vary from 2-25 mm and from 0-30 cm respectively, while the water content ranges between 0.2-12 % [28]. The proposed regression model is trained and validated within these ranges. Consequently, extrapolating this approach for cases outside the aforementioned bounds is not recommended.

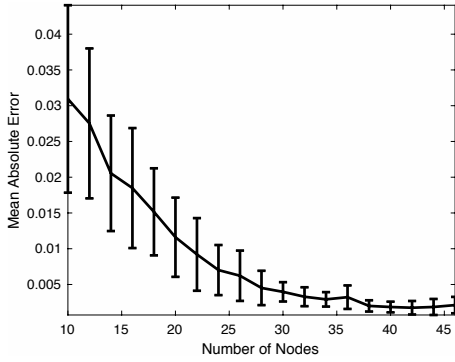


Fig. 3. The mean absolute error with respect to the number of nodes in the inner layer of the autoencoder (shown in Figure 2). The error is calculated on normalized traces. The vertical bars correspond to the standard deviation.

B. Dimensionality Reduction

High-dimensional data give rise to a complex feature space that is difficult to be resolved without large training sets and advanced learning algorithms [23], [29]. Therefore, dimensionality reduction is an essential aspect of ML, and various methodologies have been suggested for compressing the data prior to training [29]. One of the most mainstream and widely applied tool for compressing one-dimensional data is the autoencoder [30]. An autoencoder is an unsupervised NN that copies its inputs to the outputs. Autoencoders utilize the given training data $\mathbf{x} \in \mathbb{R}^n$ (n are the dimensions of the problem) and transform them to a revised representation $\mathbf{x}' \in \mathbb{R}^m$ that can be reproduced using a reduced number of dimensions (see Figure 2).

Autoencoders consist of two parts, encoders and decoders. The encoder compresses the signal through

$$\mathbf{y} = \sigma(\mathbf{A}\mathbf{x} + b) \quad (1)$$

where $\mathbf{A} \in \mathbb{R}^{m \times n}$ is the weight matrix, b is the bias, σ is the activation function, $\mathbf{y} \in \mathbb{R}^m$ is the compressed signal and m are the dimensions of the compressed signal ($m < n$). The compressed signal \mathbf{y} is then decompressed in the decoder

$$\mathbf{x}' = \sigma(\mathbf{A}'\mathbf{y} + b') \quad (2)$$

where $\mathbf{A}' \in \mathbb{R}^{n \times m}$ and b' are respectively the weight matrix and the bias of the decoder. An autoencoder can be seen as an optimization process that tries to tune \mathbf{A} , \mathbf{A}' , b and b' such as to minimize a given metric that describes the error between \mathbf{x} and \mathbf{x}' .

Figure 2 shows the autoencoder used for reducing the dimensions of the current training set. Each A-Scan consists of 300 time-steps and is compressed to 45 nodes using a single hidden layer. The number of nodes in the hidden layer (m) is chosen so as to compress the signal effectively without compromising its resolution. The activation function of each node is a rectified linear unit (ReLU) [31]. Regarding the training process, an adaptive moment estimator (Adam) [32] is used that minimises the mean squared error between \mathbf{x} and \mathbf{x}' . A subset (80%) of the data described in Section II-A is utilized during the training process, while the rest are used for testing and validation purposes. Figure 3 illustrates the error

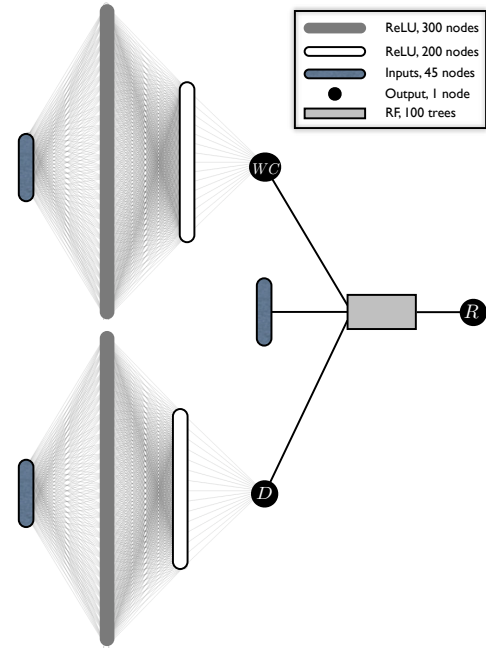


Fig. 4. The proposed detection scheme is a combination of two NNs regression models and one random forest with 100 trees. The two NNs are trained independently to evaluate the water content and the depth of the rebar based on the compressed signal. Subsequently, the estimated water content and depth are combined with the compressed A-scan and used as inputs for RF. The output of the random forest is the estimated radius of the rebar.

of the compression with respect to the number of nodes of the autoencoder. The error is calculated using data that were not used during the tuning of the autoencoder. It is apparent that the suggested compression scheme can effectively reduce the dimensions of the problem by a factor of ten without compromising the information contained within the training set.

C. Regression Scheme

The regression scheme consists of two sequential steps. In the first step, two NNs are trained to predict the water fraction of the concrete WC and the depth D of the rebar based on a single compressed A-Scan. Both NNs have two hidden layers with 300 and 200 nodes respectively, as shown in Figure 4. The activation functions of both layers are all ReLU apart from the last node which is linear. The synthetic data set is divided into three groups, 70 % of the data are used for training, while 10 % are used for validation, and 20 % for testing purposes. As with the autoencoder, Adam is employed in order to minimize the mean squared error between the actual and the estimated parameters.

In the second step, the estimated WC and D are coupled with the compressed A-Scan \mathbf{x}' to form the new input vector $\mathbf{q} = \langle WC, D, \mathbf{x}' \rangle$ (see Figure 4). Subsequently, the vector \mathbf{q} is used as input to a regression scheme based on random forest with 100 trees. Random forest is an ensemble supervised learning scheme [22] with good performance in regression problems that often surpasses NN [33]. In this work, random forest has proven to perform better than NN for estimating the

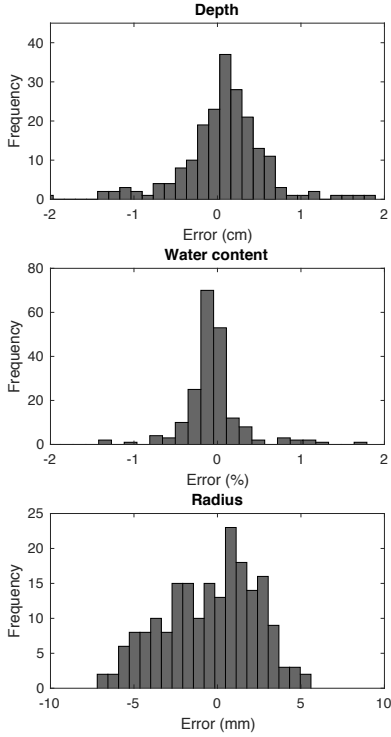


Fig. 5. Histograms of the errors between the actual and estimated parameters. The errors are calculated using unknown synthetic data, i.e. data that were not included in the training process.

diameter of the rebar. Multiple NN configurations (different layers and nodes with different activation functions and various dropout layers) were tested using different optimizers and data batches. NNs become competitive only after applying bootstrap aggregating [34], however random forest still shows better generalization capabilities when applied to real measurements.

The split criterion of the trees in the random forest tuned in this work is the mean squared error, and the nodes are expanded until all the leaves are pure. The data set is divided into training (80 %) and testing (20 %) sets, and no bootstrap was used during the training. Figure 5 illustrates the error between the actual (simulated) and the predicted (via our regression approach) parameters. The evaluation was done using unknown data that were not included in the training set. The depth D is accurately estimated with ± 2 cm maximum error and standard deviation less than ± 1 cm. The water content WC of the concrete is estimated with a maximum error at ± 2 % and standard deviation less than ± 1 %. Subsequently, the estimated D and WC are coupled with the compressed A-Scan \mathbf{x}' in order to form the input vector \mathbf{q} . Based on \mathbf{q} , the radius of the rebar is estimated with ± 6 mm accuracy. As mentioned in [11], the discrepancies between the actual and predicted radii arise due to the inherent resolution of the employed GPR antenna, which is a function of its transmitted pulse length or centre frequency (1.5 GHz). Consequently, the employed antenna has a minimum resolution (approximately 4 mm) that can not be increased with typical signal processing approaches. In order to decrease the error, we need to increase

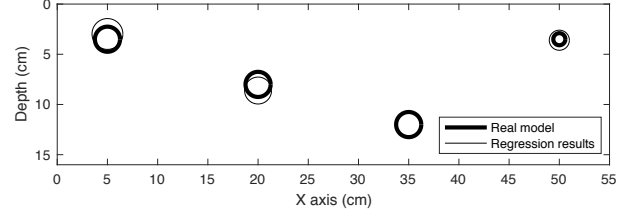


Fig. 6. The actual and the predicted rebar diameter and location using the proposed regression scheme. The inputs are real compressed A-scans collected with the antenna directly above the rebar on the surface of the (well-cured) concrete slab.

the overall resolution by employing higher frequency antennas.

From the training data, it is apparent that the developed regression is suitable for single measurements on top of the rebar. Scenarios that deviate from this setup will likely result in errors and instabilities since they would lie out of the feature space that the ML-based scheme has been trained for. Consequently, the user will initially have to identify the apex of the hyperbola and subsequently apply the ML-scheme on that trace.

III. LABORATORY EXPERIMENTS

One of the novelties of the suggested regression scheme is that it is trained entirely using synthetic data. Although synthetic data are easy to gather (compared to real data), discrepancies between the real and the numerical A-Scans will compromise machine learning and negatively affect the overall performance of the proposed approach. Accurate numerical frameworks should be employed in order for the ML to be effectively extrapolated to real measurements. Therefore, similarly to [11], special care was taken to generate synthetic but nonetheless realistic and accurate training sets [13].

Four case studies are examined in order to evaluate the generalization capabilities of the suggested scheme and validate its performance using real data. The measurements were taken in the NDT laboratory at the School of Engineering, The University of Edinburgh. Four A-Scans were collected using the GSSI 1.5 GHz antenna over four different rebars with different radii and varying depths. The polarization of the antenna was parallel with the main axis of the rebar, in the same way that the synthetic data were generated. The raw A-Scans were collected without any filtering (apart from the removal of static features) in order to match the modelled antenna [13] for which the ML was trained for.

Figure 6 shows the actual and the predicted diameters as well as the locations of the rebars. The results are given in real-time with minimum computational and operational requirements. It is apparent that both the depth and the radii of the rebars are accurately reconstructed and the errors are within the expected ranges given when using the synthetic data. The estimated water content of the concrete varies from 10.6 – 11.8% which are in excellent agreement with the ones given in [11] using FWI. This indicates that the suggested regression scheme can be successfully extrapolated to real measurements providing real-time results from a single A-scan.

IV. CONCLUSIONS

A novel regression scheme has been described that can estimate the diameter of reinforcement bars in concrete using Ground Penetrating Radar. It requires a single A-scan as an input, and provides the depth and diameter of the rebar, as well as the water content of the concrete in real-time. The regression consists of two neural networks (NNs) coupled with a random forest. Both the NNs and the random forest are trained independently using a coherent and well-labeled synthetic training dataset. The raw data were effectively compressed using a shallow autoencoder in order to reduce the dimensionality of the problem and simplify training. The resulting approach has been successfully evaluated using both numerical and real data. This demonstrates that the proposed scheme can be reliably used with real measurements, despite the fact that it has been trained entirely using synthetic data. Therefore, data-driven processing tools can complement or potentially replace multi-sensor approaches, providing an accurate and real-time method for detecting and characterizing rebars in concrete structures.

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